

INJECTIVITY OF CANONICAL MAPS BETWEEN OPERATOR SPACE TENSOR PRODUCTS

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Abstract. We establish the injectivity of the canonical inclusion from the Haagerup tensor product to the injective tensor product for operator spaces. The injectivity of the canonical maps from the operator space projective tensor product to the Haagerup, Banach space injective, and operator space injective tensor products of TROs is also proved.

Mathematics subject classification (2020): 46L06, 46L07, 46M40.

Keywords and phrases: Haagerup tensor product, operator space projective tensor product, TRO, C^* -algebras.

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