

ON THE POINT EVALUATIONS ON A CLASS OF SPACES OF HOLOMORPHIC FUNCTIONS

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Abstract. We show that it is possible to calculate norms of the point evaluation functionals on a class of spaces of holomorphic functions on the open unit disc in the complex plane that was introduced by us about two decades ago. Our main results, which are incorporated in a theorem, complement some recent results in the literature. We also present some comments and details related to the main result.

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