

VARIETY OF NUMERICAL RADIUS INEQUALITIES

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Abstract. This paper presents various bounds for the numerical radius and operator norm of bounded linear operators on a complex Hilbert space. The new results employ convexity and operator-matrix techniques in a way that allows obtaining refinements of existing results and new forms for such bounds.

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